# 1604 Cubic Eight-Puzzle

Let's play a puzzle using eight cubes placed on a  $3 \times 3$  board leaving one empty square.

Faces of cubes are painted with three colors. As a puzzle step, you can roll one of the cubes to the adjacent empty square. Your goal is to make the specified color pattern visible from above by a number of such steps. The rules of this puzzle are as follows.

1. Coloring of Cubes: All the cubes are colored in the same way as shown in Figure 3. The opposite faces have the same color.

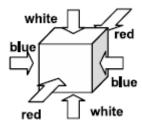


Figure 3: Coloring of a cube

2. **Initial Board State:** Eight cubes are placed on the  $3 \times 3$  board leaving one empty square. All the cubes have the same orientation as shown in Figure 4. As shown in the figure, squares on the board are given x and y coordinates,  $(1, 1), (1, 2), \ldots$ , and (3, 3). The position of the initially empty square may vary.

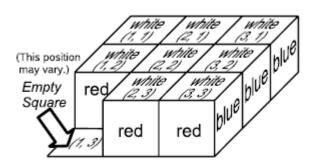


Figure 4: Initial board state

3. **Rolling Cubes:** At each step, we can choose one of the cubes adjacent to the empty square and roll it into the empty square, leaving the original position empty. Figure 5 shows an example.

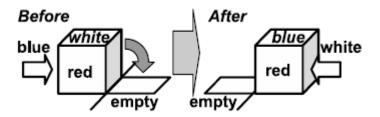


Figure 5: Rolling a cube

4. **Goal:** The goal of this puzzle is to arrange the cubes so that their top faces form the specified color pattern by a number of cube rolling steps described above.

Your task is to write a program that finds the minimum number of steps required to make the specified color pattern from the given initial state.

#### Input

The input is a sequence of datasets. The end of the input is indicated by a line containing two zeros separated by a space. The number of datasets is less than 16. Each dataset is formatted as follows.

```
\begin{array}{cccc} x & y \\ F_{11} & F_{21} & F_{31} \\ F_{12} & F_{22} & F_{32} \\ F_{13} & F_{23} & F_{33} \end{array}
```

The first line contains two integers x and y separated by a space, indicating the position (x, y) of the initially empty square. The values of x and y are 1, 2, or 3.

The following three lines specify the color pattern to make. Each line contains three characters  $F_{1j}$ ,  $F_{2j}$ , and  $F_{3j}$ , separated by a space. Character  $F_{ij}$  indicates the top color of the cube, if any, at position (i, j) as follows:

```
B: Blue,
```

W: White,

R: Red,

E: the square is Empty.

There is exactly one 'E' character in each dataset.

#### Output

For each dataset, output the minimum number of steps to achieve the goal, when the goal can be reached within 30 steps. Otherwise, output '-1' for the dataset.

### Sample Input

1 2

W W

E W W

W W W

2 1

R B W

R W W

E W W

3 3

W B W

BRE

R B R

3 3

B W R

B W R

- B E R
- 2 1
- В В В
- B R B
- $B\ R\ E$
- 1 1
- R R R
- W W W
- R R E
- 2 1
- R R R
- B W B
- R R E
- 3 2
- R R R
- W E W
- R R R
- 0 0

## Sample Output

- 0
- 3
- 13
- 23 29
- \_\_
- 30
- -1 -1